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WHAT'S REAL ABOUT THE BUSINESS CYCLE?

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ABSTRACT

This paper argues that a linear statistical model with homoskedastic errors cannot capture the nineteenth-century notion of a recurring cyclical pattern in key economic aggregates. A simple nonlinear alternative is proposed and used to illustrate that the dynamic behavior of unemployment seems to change over the business cycle, with the unemployment rate rising more quickly than it falls. Furthermore, many but not all economic downturns are also accompanied by a dramatic change in the dynamic behavior of short-term interest rates. It is suggested that these nonlinearities are most naturally interpreted as resulting from short-run failures in the employment and credit markets, and that understanding these short-run failures is the key to understanding the nature of the business cycle.

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1 What is the business cycle?

The term “cycle” is used to describe a process that moves sequentially between a series of clearly identifiable phases in a recurrent or periodic fashion. Economists of the nineteenth and early twentieth centuries were persuaded that they saw such a pattern exhibited in the overall level of economic activity, and enthusiastically sought to characterize the observed regularities of what came to be known as the “business cycle.” The most systematic and still enduring summaries of what seems to happen during the respective phases were provided by Mitchell (1927, 1951) and Burns and Mitchell (1946).

The expression “business cycle theory” remains in common usage today, even though, in most of the modern models that wear the label, there in fact is no business cycle in the sense just described. These are models of economic fluctuations, to be sure, but they do not exhibit clearly articulated phases through which the economy could be said to pass in a recurrent pattern.

In part this shift in the profession’s conception of what needs to be explained about business fluctuations reflects a desire to integrate the determinants of long-run economic growth and the causes of short-run economic downturns within a single unified theory of aggregate economic performance. Since improvements in overall productivity are widely acknowledged to be one of the key factors driving long-run growth, and since such improvements cannot reasonably be expected to occur at a constant rate over time, it is natural to explore the possibility that variation over time in the rate of technological progress could be a primary cause of variation over time in the level of economic activity. Brock and Mirman

(1972) were the first to incorporate stochastic variation in the rate of technical progress into a neoclassical growth model, though they clearly intended this as a model of long-run growth rather than a realistic description of short-run fluctuations. Kydland and Prescott (1982) later took the much bolder step of proposing that this class of models might explain variations in economic activity at all frequencies, in what has come to be known as “real business cycle models.”

Although unifying growth and business cycle theory holds tremendous aesthetic appeal, this particular solution is not without its detractors. Indeed, the reasons that Irving Fisher gave in 1932 for rejecting such an approach have in the opinion of many yet to receive a satisfying response from modern real business cycle theorists:

“... in times of depression, is the soil less fertile? Not at all. Does it lack rain? Not at all. Are the mines exhausted? No, they can perhaps pour out even more than the old volume of ore, if anyone will buy. Are the factories, then, lamed in some way—down at the heel? No; machinery and invention may be at the very peak.” (Fisher, 1932, p. 5)

Continuing along the lines of Fisher’s reasoning, the size of the population places an obvious physical limit on how much a given nation can produce, and is certainly a key factor responsible for an increase in aggregate output over time. But just as surely, a decrease in population is not the cause of the decrease in employment that we observe in times when the unemployment rate is shooting up dramatically. There is in this respect an obvious inherent asymmetry in fluctuations in the number of workers employed— the measure must

go up for different reasons than it goes down. A parallel argument can be made in terms of the capital stock, another key factor determining long-run growth which again places an upper limit on how much a country can produce. Yet in times when we see all measures of capacity utilization falling, the natural inference is that some forces other than the quantity or quality of available manufacturing facilities account for the drop in aggregate output.

If we agree that these three factors— technology, labor force, and the capital stock— are the three main determinants of long-run economic growth, we might greet with considerable skepticism the suggestion that the same three factors are in a parallel way responsible for producing the drop in real GDP that we observe during a business downturn.

The purpose of this paper is to explore whether the nineteenth-century economists were on to something that their modern descendants may have forgotten. Is there really a business cycle, or is the expression an unfortunate linguistic vestige of a less-informed era? I will argue that indeed there is a recurring pattern in the level of economic activity that needs to be explained, but that a statistical characterization of this pattern requires a nonlinear dynamic representation and calls for an asymmetric interpretation of the forces that cause employment to rise and fall. I further observe that one element of this pattern has often been a related cyclical behavior of interest rates.

To the question, “Is the business cycle real?”, these findings suggest that yes, the business cycle is real in the sense that it is a feature of the data that needs to be explained. In the other meaning of the term “real,” however— the sense from which springs the label “real business cycle,” namely, a cycle unrelated to monetary developments— the evidence ad-

duced here for the importance of comovements between financial and real variables suggests that the cycle is not “real” at all, or at the least, not completely divorced from monetary developments.

2 The behavior of unemployment.

Figure 1 plots the monthly unemployment rate in the U.S. from 1948:1 to 2004:3.¹ I would suggest that someone looking at such a graph for the first time would indeed be inclined to identify a repeated sequence of ups and downs, with each of the obvious sharp upswings in the unemployment rate occurring during periods that the National Bureau of Economic Research has classified as economic recessions (indicated by shaded regions on the graph).

Although one’s eye is sympathetic to the claim that these data display a recurrent pattern, it does not appear to be cyclical in the sense of exhibiting strict periodicity. For example, the two consecutive unemployment peaks in 1958:7 and 1961:5 are separated by less than three years, whereas those of 1982:11 and 1992:6 are separated by a decade. More formally, one can look for any sort of periodic pattern by examining the spectrum of the unemployment rate, an estimate of which is plotted in Figure 2 as a function of the period of the cycle.² If one tries to decompose the unemployment series in Figure 1 into a series of strictly periodic

¹ This is the seasonally adjusted civilian unemployment rate from the Bureau of Labor Statistics (<http://stats.bls.gov>).

² This was calculated by smoothing the sample periodogram with a Bartlett window (e.g., Hamilton, 1994, eq. [6.3.15]) with lag $q = 13$, as calculated using the RATS fft procedure with `window(type=tent, width=25)`. See the procedure `hamp167.prg` available at http://www.estima.com/procs_hamilton.shtml for details. The resulting estimate $\hat{s}_Y(\omega_j)$ for $\omega_j = 2\pi j/T$ is plotted in Figure 2 for given j as a function of T/j , which is the variable measured on the horizontal axis.

cycles, by far the most important of these are those with the longest period, as opposed to something regularly repeating every 3 to 5 years.

Let y_t denote the unemployment rate. Consider an AR(2) representation of these data with Student t innovations, obtained by maximizing the log likelihood function

$$\mathcal{L}(\boldsymbol{\theta}) = \sum_{t=3}^T \mathcal{l}_t(\boldsymbol{\theta})$$

$$\mathcal{l}_t(\boldsymbol{\theta}) = k - [(\nu + 1)/2] \log \left[1 + \frac{u_t^2}{\nu \sigma^2} \right] \quad (1)$$

$$u_t = y_t - c - \phi_1 y_{t-1} - \phi_2 y_{t-2} \quad (2)$$

$$k = \log \{ \Gamma [(\nu + 1)/2] \} - \log \{ \Gamma [\nu/2] \} - (1/2) \log(\sigma^2 \nu \pi) \quad (3)$$

with respect to $\boldsymbol{\theta} = (c, \phi_1, \phi_2, \sigma^2, \nu)'$ subject to the constraints³ that $\sigma^2 > 0$ and $\nu > 0$.

These maximum likelihood estimates (with asymptotic standard errors in parentheses) imply that the unemployment rate y_t for month t could be modeled as follows

$$y_t = \underset{(0.028)}{0.060} + \underset{(0.037)}{1.117} y_{t-1} - \underset{(0.037)}{0.128} y_{t-2} + \underset{(0.007)}{0.158} v_t \quad (4)$$

where v_t is distributed Student t with 4.42 degrees of freedom, with the standard error for the degrees-of-freedom parameter ν being estimated at 0.74. Using Student t innovations instead of Normal increases the log likelihood by 52.04, a huge gain from estimating the single parameter ν ; (see Table 1).

As further evidence against a cycle with regular periodicity, it is interesting to note that the roots of the second-order difference equation in (4) are both positive and real, meaning that this system does not exhibit any oscillatory behavior in response to a shock to v_t .

³ See for example Hamilton (1994, Section 5.9) on numerical maximization subject to inequality constraints.

Is the appearance of a repeated cycle in Figure 1 just a figment of our imagination, then? Another interesting exercise is to simulate a time series realization from (4), which is displayed in Figure 3. These simulated data have the same mean, variance, and serial correlation as the real data in Figure 1, as of course they should. Even so, one has little of the sense of a recurrent cycle in these simulated data that seemed compelling in the actual data. If one were to label some of the episodes in this simulated data set as “recessions,” where would they be? Indeed, expression (4) characterizes the true process from which these artificial data were simulated. What in terms of the qualities of this data-generating process would one characterize as a “business cycle?” There are good and bad values of the innovations v_t , and perhaps we could make up some rule for categorizing a relatively unlikely string of mostly negative innovations as a “recession.” But any such rule would be completely arbitrary, and tell us more about our imagination or quest for patterns and labels than about anything in the objective reality. There is nothing qualitatively different about a value of v_t that puts us within the arbitrary recession category and one that leaves us just short of it.

I would argue that this inability to define a business cycle as a fundamental attribute of the data-generating process (4) is in fact inherent in any time series model that describes y_t as a linear function of its lagged values plus an i.i.d. innovation. Even if the linear difference equation did exhibit an oscillatory impulse-response function or imply more power in the spectrum at periods of 3-5 years, it seems to be some other feature of the data in Figure 1 that constitutes the “business cycle.”

I would suggest instead that what we have in mind is that there is something in common between the rapid run-ups in unemployment that occurred in each of the postwar recessions, even though the length of time it takes for unemployment to spike up varies from episode to episode, and the timing separating such events is irregular. Indeed, the idea of looking for commonality across recessions whose elapsed calendar time is different for different episodes was precisely the methodology that Burns and Mitchell used to create their graphs summarizing typical business cycle patterns. Stock (1987, 1988) showed that such a way of thinking about data necessarily implies a nonlinear data-generating process. Friedman (1969, p. 274) and DeLong and Summers (1986), among others, have forcefully advanced the related proposition that asymmetry is the defining characteristic of business cycles. In particular, the asymmetry commented on in Figure 1— that recessions are characterized by an unusually rapid but nonetheless transient increase in the unemployment rate— has been confirmed to be a statistically significant feature of these data in a number of recent quantitative studies, including Montgomery, et. al. (1998), Rothman (1998), and van Dijk, Franses, and Paap (2002).

Suppose we try in a simple way to represent the asymmetry that the eye perceives in Figure 1. One idea is that the intercept in equation (2) assumes different values in different phases of the business cycle. Consider the following generalization of (2),

$$y_t = c_{s_t} + \phi_1 y_{t-1} + \phi_2 y_{t-2} + u_t, \quad (5)$$

where $s_t = 1$ if the economy is in the normal growth state at date t , $s_t = 2$ if it is in a mild recession, and $s_t = 3$ for a severe recession. Suppose that the transition between these three

regimes follows a Markov chain, with $p_{ij} = \Pr(s_t = j | s_{t-1} = i)$ another set of 9 parameters to be estimated subject to the constraints $0 \leq p_{ij} \leq 1$ and $\sum_{j=1}^3 p_{ij} = 1$. Conditional on the economy being in regime j at date t , the unemployment rate thus has conditional log density given by

$$\log f(y_t | s_t = j, y_{t-1}, y_{t-2}, \dots, y_1) = k - [(\nu + 1)/2] \log \left[1 + \frac{u_{jt}^2}{\nu \sigma^2} \right]$$

$$u_{jt} = y_t - c_j - \phi_1 y_{t-1} - \phi_2 y_{t-2}$$

for k as in (3).

The log likelihood for the observed data,

$$\mathbf{L}(\boldsymbol{\theta}) = \sum_{t=3}^T \log f(y_t | y_{t-1}, y_{t-2}, \dots, y_1; \boldsymbol{\theta})$$

can then be calculated as in Hamilton (1994, equation [22.4.7]) and maximized numerically with respect to the population parameters $\boldsymbol{\theta} = (c_1, c_2, c_3, \phi_1, \phi_2, \sigma, \nu, p_{11}, p_{12}, p_{13}, p_{21}, p_{22}, p_{23}, p_{31}, p_{32}, p_{33})'$. The maximum likelihood estimates turn out to be at the boundaries such that $p_{13} = 0$ and $p_{31} = 0$, that is, states 1 and 3 never follow each other. These maximum likelihood estimates are reported in Table 2, where in order to calculate standard errors from the second derivative matrix of the log likelihood, we went ahead and imposed the constraint $p_{13} = p_{31} = 0$ so that there are just 4 free transition probabilities (p_{11}, p_{21}, p_{22} , and p_{32}). The smoothed probabilities implied by the maximum likelihood estimates, $\Pr(s_t = j | y_1, y_2, \dots, y_T; \hat{\boldsymbol{\theta}})$, are plotted in Figure 4.

Note that allowing this nonlinearity produces a further huge improvement in the log likelihood and would easily be selected on the basis of the Schwarz criterion (again see Table

1). Formal tests of the null hypothesis of no Markov-switching have been proposed by Hansen (1992), Hamilton (1996), Garcia (1998), and Carrasco, Hu, and Ploberger (2004). The latter have found the optimal test against the alternative of Markov-switching, which we implement here for the special case where the alternative to (4) is a model with Markov-switching in the intercept only as in (5); for details of the Carrasco, Hu, and Ploberger test see the appendix. The test statistic on the U.S. employment data turns out to be 26.02, whereas the 5% critical value is only 4.01, providing overwhelming evidence for representing the data with the model described in Table 2 rather than (4).

Consider some of the properties of the estimated Markov-switching model. The process is stationary, allowing us to take the unconditional expectation of equation (5),

$$E(y_t) = \sum_{j=1}^3 c_j \Pr(s_t = j) + \phi_1 E(y_t) + \phi_2 E(y_t)$$

implying

$$E(y_t) = (1 - \phi_1 - \phi_2)^{-1} \sum_{j=1}^3 c_j \Pr(s_t = j). \quad (6)$$

The ergodic probabilities can be calculated as in Hamilton (1994, equation [22.2.26]):

$$\begin{bmatrix} \Pr(s_t = 1) \\ \Pr(s_t = 2) \\ \Pr(s_t = 3) \end{bmatrix} = \begin{bmatrix} 0.810 \\ 0.165 \\ 0.025 \end{bmatrix}.$$

In other words, the economy spends about 80% of the time in the normal phase of the business cycle. Substituting these unconditional probabilities into (6), the model implies an expected unemployment rate of 5.9%, close to the postwar average.⁴ If the economy is in

⁴ Unlike ordinary least squares, the maximum likelihood estimates in this case do not imply an estimate

state i at date t , on average it will stay there for $\sum_{k=1}^{\infty} (1 - p_{ii})^k p_{ii}^{k-1} = (1 - p_{ii})^{-1}$ months.

From the transition probabilities in Table 2, the expected duration of each regime is

$$\begin{bmatrix} (1 - p_{11})^{-1} \\ (1 - p_{22})^{-1} \\ (1 - p_{33})^{-1} \end{bmatrix} = \begin{bmatrix} 34.0 \\ 4.5 \\ 2.0 \end{bmatrix}.$$

A typical expansion thus might last about 3 years. A mild recession often lasts less than half a year, at which point it might enter the more severe phase for a few months, and then spend another half year again at moderately high unemployment rates before coming back down.

Figure 5 displays the way in which this representation captures the asymmetry of the business cycle discussed above. Suppose the economy is currently experiencing an unemployment rate of 6% but is in the recovery phase of the cycle ($s_t = 1$). In the absence of any new shocks ($u_{t+j} = 0$ for all j), the dynamic behavior of the unemployment rate over time would be given by

$$y_{t+j} = 0.0605 + 0.8584y_{t+j-1} + 0.1217y_{t+j-2}$$

for $j = 1, 2, \dots$ starting from $y_t = y_{t-1} = 6.0$. The top panel of Figure 5 plots this path for y_{t+j} as a function of j . The unemployment rate falls quite gradually in this phase. If the phase persisted indefinitely, the unemployment rate would eventually stabilize at a value of

$$0.0605 / (1 - 0.8584 - 0.1217) = 3.04,$$

of the population mean that is equal by construction to the sample mean.

though it would take 30 years of expansion to get there; in the first year of the expansion, the unemployment rate would only drop 0.6%.

By contrast, if the economy started with $y_t = 3.0$ and entered the mild recession phase, the unemployment rate would rise much more quickly than it fell, reaching 5.4% within a year (see Panel B of Figure 5). And if the economy starts with unemployment at 6% and enters the severe recession phase (Panel C), the rate would reach nearly 12% after a year.

This asymmetry in unemployment dynamics is subtle in the statistical sense that the baseline model (4) adequately captures most of the gross features of the data. But it seems extremely important from an economic perspective. For once we agree that up and down movements in the unemployment rate occur at different speeds, the notion that they may be caused by different economic forces becomes much more appealing. Finding this kind of nonlinearity using modern statistical methods could thereby be interpreted as exonerating to some degree the assumptions of early students of the business cycle. Specifically, it suggests that there is a real event associated with the label of an “economic recession,” which is measurable by objective statistical methods as a change in the dynamic behavior of the unemployment rate. It further suggests that the key task for business cycle theorists should not be to look for a unification between the explanation of short-run dynamics and long-run growth, but rather to identify the factors that can result in a temporary failure of the economy to utilize efficiently the available labor, capital, and technology.

3 The behavior of interest rates.

I argued above that the business cycle is not an artificial categorization existing only in the imagination of economists but rather is an integral part of the real data-generating process. In addition to believing that such patterns exist, early students of the business cycle also differed from their modern counterparts in the degree to which financial factors were viewed as a key part of the business cycle. For example, Burton (1902) described the typical business downturn in the following terms:

“The usual signal for the beginning of a crisis is a conspicuous banking or mercantile failure, or the exposure of some fraudulent enterprise which attracts widespread attention. Money is hoarded. Credit is refused.” (Burton, 1902)

As a first look at some of the evidence that may have inspired such an opinion, consider Figure 6, which plots the series on commercial paper rates in New York city compiled by Macaulay (1938).⁵ These data behave very differently before and after the founding of the U.S. Federal Reserve in 1913, a point to which we will want to return shortly. But first consider the behavior of this series prior to 1913. There is at least one asymmetry that Figure 1 and Figure 6 have in common, induced per force by the fact that neither the unemployment rate nor the nominal interest rate can ever go negative, but both can go and occasionally have gone quite far above their usual levels. Notwithstanding, interest rates do not display the same obvious pattern of ups and downs as the unemployment data in Figure

⁵ Taken from Macaulay (1938, Column 3, Table 10, pp. A142-161. Macaulay describes these as “choice 60-90 day two name paper” up to 1923 and “four to six month prime double and single name paper” from 1924 on.

1. Indeed, apart from seasonal fluctuations stemming from the predominance of agriculture in the economy over this period, such predictable swings might be difficult to reconcile with the view that asset markets function efficiently given investors' ability to arbitrage between securities of different maturities. Nevertheless, there are a number of interest-rate spikes prior to 1913 that are quite dramatic visually and that have been delegated particular names as important points of reference for economic historians, names such as the Crisis of 1857, Crisis of 1873, or the Panic of 1893.

As in the case of postwar unemployment rates, there is no obvious periodicity to the occurrence of these interest rate spikes. Figure 7 plots the spectrum of interest rates over the 1857:1 to 1913:12 period, which again is dominated by the lowest frequencies. There is a noticeable local peak associated with cycles of a 12-month period, reflecting the tendency of interest rates to be highest in the winter months when agricultural borrowing needs were greatest. But again there is no mass whatever for what are often described as "business cycle frequencies," namely cycles with periods of 3 to 5 years.

For a baseline model, we estimated a slight generalization of the model in equations (1)-(3) to allow for a possible seasonal pattern in interest rates, replacing equation (2) with

$$u_t = z_t - \phi_1 z_{t-1} - \phi_2 z_{t-2} \tag{7}$$

$$z_t = y_t - c - \gamma \cos(\pi t/6)$$

for y_t now the interest rate and $t = 1$ corresponding to the January 1857 observation. A positive value of γ would reflect the tendency for interest rates to peak around December. The likelihood was then maximized numerically over 1857:3 to 1913:12, resulting in the

estimates reported in Table 3. Once again allowing Student t innovations implies a huge improvement in the log likelihood over a Gaussian specification (see Table 4).

Apart from the seasonal cycle in agriculture, economic theory would lead us to expect that changes in interest rates are much harder to forecast than the unemployment rate. A Markov-switching specification related to that in (5) is to allow the variance rather than the intercept to change with the regime, so that the conditional log density of the t th observation is

$$\log f(y_t | s_t = j, y_{t-1}, y_{t-2}, \dots, y_1) = k_j - [(\nu + 1)/2] \log \left[1 + \frac{u_t^2}{\nu \sigma_j^2} \right]$$

$$k_j = \log \{ \Gamma [(\nu + 1)/2] \} - \log \{ \Gamma [\nu/2] \} - (1/2) \log(\sigma_j^2 \nu \pi)$$

where u_t is again given by (7). Here we allow only two regimes, with the scale parameter taking the value σ_1 in the low-variance regime and σ_2 in the high-variance regime.

As seen in Table 4, allowing the possibility of changes in the variance parameter over time again leads to a very big improvement in the fit to the data. We can also again use the Carasco, Hu, and Ploberger test, this time constructed for the alternative of a Markov-switching variance, as described in the appendix. The test statistic is 63.34, which vastly exceeds the 5% critical value of 3.68, and indeed exceeds the largest value (19.28) among any of our 1000 Monte Carlo simulations.

The maximum likelihood estimates are reported in Table 5. Regime 2 is characterized by a variance of interest rate innovations that is thrice that for regime 1, with the ergodic probabilities implying that the economy would spend about 80% of the time in the low-variance regime. Smoothed probabilistic inferences about when U.S. interest rates were

unusually volatile are graphed in the middle panel of Figure 8, and repeated in the bottom graph for comparison with NBER-dated recessions (shown as shaded regions) over this period. Those dates for which the smoothed probability of being in the high-variance regime, $\Pr(s_t = 2|y_1, y_2, \dots, y_T; \hat{\theta})$, exceeds one-half are categorized in Table 6 as episodes of unusually volatile interest rates for further comparison with the dates NBER has ascribed to economic recessions.⁶ The correspondence between these two sets of dates is strong, but not perfect. There are a half-dozen recessions in the 1880's and early 1900's when nothing much was happening to interest rates, and one interest rate spike (in 1898) which comes in the middle of an economic expansion. A long episode of interest rate volatility in the late 1860's and early 1870's also correlates rather weakly with the recessions at those times. On the other hand, there are a number of other recessions, notably those of 1857-58, 1860-61, 1893, and 1896, which match up perfectly with very dramatic shifts in the interest rate regime. The suggestion thus seems strong that an important shift in the interest rate process is indeed related to some but by no means all of the 19th-century economic downturns.

The asymmetry found in unemployment dynamics— that unemployment rises above its average rate more quickly than it falls below its average rate— seemed to suggest rather directly that macroeconomic theorists should be looking for different explanations as to why employment rises and falls. By contrast, the deficiency of a homoskedastic linear model as a description of 19th-century interest rate dynamics— that interest rates are much more volatile at some times than others— would be consistent with any model that implies GARCH

⁶ These can be found at <http://www.nber.org/cycles/cyclesmain.html>.

effects on interest rates.⁷ However, it does seem fair to describe this finding as implying that, at least during some of the 19th-century recessions, interest rates were being influenced by some forces that are not operating in usual times, or, perhaps more strongly, that the financial crises emphasized by early students of the business cycle are in some important respects qualitatively different from the factors governing normal interest rate fluctuations.

It is quite apparent from Figure 6 that the behavior of short-term interest rates changed dramatically after the Federal Reserve Act in 1913, as both the seasonality and the sharp spikes in interest rates were successfully eliminated.⁸ However, a few broad surges in interest rates after the founding of the Fed are certainly identifiable in the post-Fed data. These precede the economic downturn of 1920-21 and the Great Depression beginning in 1929, in addition to a minor spike coinciding with the worsening economic situation in 1931.⁹ This post-Fed correlation led many economists to conclude that the contribution of liquidity crunches to economic downturns did not end with the founding of the Federal Reserve.

Indeed, there is some indication that this pattern is a characteristic of postwar business cycles as well. The top panel of Figure 9 displays U.S. 6-month Treasury bill rates¹⁰ from 1958:12 to 2004:4 along with U.S. recessions as shaded areas. Again one's eye is tempted to see a recurrent tendency for the interest rate to surge upward prior to every postwar

⁷ See for example Granger and Machina (2004).

⁸ See Miron's (1986) interesting discussion of the possible relation between these two facts.

⁹ Among the many discussing these events are Friedman and Schwartz (1963) and Hamilton (1987, 1988).

¹⁰ These are averages over business days during the month from the secondary market. Data are from the FRED data base of the Federal Reserve Bank of St. Louis.

recession, though the pattern is more convincing for some recessions than for others.

Bansal and Zhou (2002), Ang and Bekaert (2002) and Dai, Singleton, and Yang (2003) have used a Markov-switching framework to suggest that a connection between interest rate volatility and economic recessions also characterizes postwar data. We applied the method used to analyze 19th-century interest rates to postwar data, with two changes. First, the term representing the agricultural seasonal was dropped. Second, we estimated the model in differences rather than levels. The reason is that levels estimation results in one root that is virtually unity, which would very rarely introduce numerical problems with maximizing the log likelihood for simulated samples in the Monte Carlo calculation of the Carrasco, Hu, and Ploberger statistic (though results reported below are otherwise identical for estimation in either levels or differences).

Table 7 replicates the findings on our other two data sets: the data are far better described with Student t as opposed to Normal innovations, and further allowing for Markov-switching in the variance yields a further huge improvement in fit. Again the Carrasco, Hu, and Ploberger statistic of 137.38 far exceeds the 95% critical value of 4.03 and indeed any value in our 1000 Monte Carlo simulated samples.

Maximum likelihood estimates are reported in Table 8. The standard deviation of the innovation is four times as big in regime 2 compared to regime 1. The bottom panel of Figure 9 plots the smoothed probability that the economy was in the high-volatility regime for each month. As in the 19th-century data, there appears to be a clear connection between interest rate volatility and economic recessions, at least for the recessions of 1973-75, 1980, and 1981-

82, confirming Bansal and Zhou’s (2002), Ang and Bekaert’s (2002) and Dai, Singleton, and Yang’s (2003) conclusions from the volatility of the term structure.

Nor is this pattern unique to the United States. For example, Neumeyer and Perri (2004) noted that domestic interest rate spikes preceded the strong economic downturns in Mexico in 1994, Brazil and Argentina in 1995, and Korea and the Philippines in 1997, each of which had important similarities with the financial crises seen repeatedly in the United States in the nineteenth century.

4 Conclusion.

We now return to the question posed in the title of this paper, “What’s real about the business cycle?” If an accurate statistical description of the dynamic behavior of key economic magnitudes is a time-invariant linear model such as equation (4), then the correct answer is, there is no such thing as a business cycle. In this case, we might as well stop using the phrase “the business cycle,” inherited from a less-informed century, and continue with our efforts at trying to describe short-run economic fluctuations as being governed by the same factors that determine long-run economic growth.

However, we’ve encountered substantial statistical evidence that there are some features of both unemployment and interest-rate dynamics that are inconsistent with a time-invariant linear specification. Each of these series seems to exhibit different dynamic behavior in recessions and expansions. The unemployment rate rises more quickly than it falls, and this often occurs at the same time as rapid spikes up and then back down in short-term

interest rates. If moving between such episodes is indeed what we mean by “the business cycle,” then the correct answer to our question is, the business cycle is very much a real, objectively measurable phenomenon, in which case keeping both the phrase as well as the research program that the expression invites seems well worth while.

The paper’s title is of course also a play on words, insofar as “real business cycle theory” is derived from a class of models in which short-run economic fluctuations are driven by the same real (i.e., nonmonetary) factors that are responsible for long-run growth. Our findings cast some doubt on the claim that the business cycle is “real” in this sense. The observation that the dynamics change over the course of the business cycle suggests instead that the forces that cause employment to rise may be quite different from those that cause it to fall. Furthermore, the coincidence of this phenomena with large rapid moves in interest rates suggests that something is disrupting the normal functioning of both labor and financial markets. It is difficult to reconcile these facts with a world view in which financial markets play no role in economic fluctuations.

Appendix: The Carrasco, Hu, and Ploberger Test for Markov Switching

As in equation (1), let $l_t(\boldsymbol{\theta})$ denote the conditional log likelihood of the t th observation under the null hypothesis of no Markov-switching, and let $l_t^{(1)}(\boldsymbol{\theta})$ and $l_t^{(2)}(\boldsymbol{\theta})$ denote its first and second derivatives with respect to the intercept c :

$$l_t^{(1)}(\boldsymbol{\theta}) = z_t u_t \quad (8)$$

$$l_t^{(2)}(\boldsymbol{\theta}) = -z_t + \frac{2z_t^2 u_t^2}{\nu + 1} \quad (9)$$

where

$$z_t = \frac{\nu + 1}{\nu \sigma^2 + u_t^2}.$$

Define

$$\gamma_t(\rho; \hat{\boldsymbol{\theta}}) = l_t^{(2)}(\hat{\boldsymbol{\theta}}) + \left[l_t^{(1)}(\hat{\boldsymbol{\theta}}) \right]^2 + 2 \sum_{s < t} \rho^{t-s} l_t^{(1)}(\hat{\boldsymbol{\theta}}) l_s^{(1)}(\hat{\boldsymbol{\theta}})$$

where ρ is a nuisance parameter characterizing the serial correlation of the Markov chain for s_t under the alternative hypothesis of Markov switching. Finally, let $\mathbf{h}_t(\hat{\boldsymbol{\theta}})$ denote the entire vector of derivatives evaluated at the MLE, of which $l_t^{(1)}(\hat{\boldsymbol{\theta}})$ is the first element,

$$\mathbf{h}_t(\hat{\boldsymbol{\theta}}) = \left. \frac{\partial l_t(\boldsymbol{\theta})}{\partial \boldsymbol{\theta}} \right|_{\boldsymbol{\theta}=\hat{\boldsymbol{\theta}}} = \begin{bmatrix} z_t \hat{u}_t \mathbf{x}_t \\ -\frac{1}{2\hat{\sigma}^2} + \frac{z_t \hat{u}_t^2}{2\hat{\sigma}^2} \end{bmatrix},$$

for $\mathbf{x}_t = (1, y_{t-1}, y_{t-2})'$ and let $\hat{\varepsilon}_t(\rho; \hat{\boldsymbol{\theta}})$ denote the residual from an OLS regression of $(1/2)\gamma_t(\rho; \hat{\boldsymbol{\theta}})$ on $\mathbf{h}_t(\hat{\boldsymbol{\theta}})$. Carrasco, Hu, and Ploberger proposed calculating

$$C(\rho; \hat{\boldsymbol{\theta}}) = \left[\max \left\{ 0, \frac{\sum_{t=1}^T \gamma_t(\rho)}{2 \sqrt{\sum_{t=1}^T \left[\hat{\varepsilon}_t(\rho; \hat{\boldsymbol{\theta}}) \right]^2}} \right\} \right]^2 \quad (10)$$

and finding the maximum value of $C(\rho; \hat{\boldsymbol{\theta}})$ over a fixed range of alternatives, say $\rho \in [0.2, 0.8]$.

In my applications this was achieved by calculating the value of

$$v(\lambda; \hat{\boldsymbol{\theta}}) = \frac{\sum_{t=1}^T \gamma_t(\rho(\lambda); \hat{\boldsymbol{\theta}})}{2\sqrt{\sum_{t=1}^T [\hat{\varepsilon}_t(\rho(\lambda)); \hat{\boldsymbol{\theta}}]^2}}$$

for

$$\rho(\lambda) = 0.2 + 0.6 \frac{|\lambda|}{\sqrt{1 + \lambda^2}}$$

and maximizing $v(\lambda; \hat{\boldsymbol{\theta}})$ numerically with respect to λ .

Critical values for the test statistic ν were obtained by parametric bootstrap as follows. A total of $M = 1000$ samples each of size $T = 673$ were generated from (4). For the m th artificial sample, the maximum likelihood estimate $\hat{\boldsymbol{\theta}}^{(m)}$ was found by numerical search for that sample and then the function $\nu(\lambda; \hat{\boldsymbol{\theta}}^{(m)})$ was maximized numerically with respect to λ . The p -value of the observed statistic for the original sample $\nu(\lambda^*, \hat{\boldsymbol{\theta}})$ was then estimated from the fraction of the m samples for which $\nu(\lambda^{*(m)}, \hat{\boldsymbol{\theta}}^{(m)})$ exceeded $\nu(\lambda^*, \hat{\boldsymbol{\theta}})$.

To test the null of constant regimes against the alternative of Markov-switching in the variance, we replace (8) and (9) with

$$\begin{aligned} l_t^{(1)}(\boldsymbol{\theta}) &= -\frac{1}{2\sigma^2} + \frac{z_t u_t^2}{2\sigma^2} \\ l_t^{(2)}(\boldsymbol{\theta}) &= \frac{1}{2\sigma^4} - \frac{z_t u_t^2}{2\sigma^4} - \frac{z_t^2 u_t^2 \nu}{2\sigma^2(\nu + 1)}. \end{aligned}$$

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Table 1

Comparison of selected models of postwar unemployment rates

Model	# of parameters	Log likelihood	Schwarz criterion
Gaussian AR(2)	4	75.59	62.57
Student t AR(2)	5	127.63	111.35
Student t AR(2) with MS intercept	11	174.58	138.77

Note: Schwarz criterion calculated as $L - (k/2) \log(T)$ for L the log likelihood, k the number of parameters, and $T = 673$ the sample size.

Table 2

Maximum likelihood estimates of 3-state Markov-switching model for postwar unemployment rate

symbol	explanation	MLE	std error
c_1	normal intercept	0.0605	0.0294
c_2	mild recession intercept	0.307	0.038
c_3	severe recession intercept	0.715	0.075
ϕ_1	first AR coefficient	0.8584	0.0371
ϕ_2	second AR coefficient	0.1217	0.0366
σ	standard dev/scale	0.134	0.007
ν	degrees of freedom	5.09	1.01
$[p_{ij}]$	state transition probs	$\begin{bmatrix} 0.971 & 0.145 & 0 \\ 0.029 & 0.778 & 0.508 \\ 0 & 0.077 & 0.492 \end{bmatrix}$	$\begin{bmatrix} 0.010 & 0.046 & - & - & - \\ 0.010 & 0.065 & 0.193 & & \\ - & - & - & 0.041 & 0.193 \end{bmatrix}$

Table 3

Maximum likelihood estimates of baseline model for 19th-century interest rates

symbol	explanation	MLE	std error
c	typical interest rate	5.11	0.18
ϕ_1	first AR coefficient	1.104	0.031
ϕ_2	second AR coefficient	-0.212	0.026
γ	effect of seasonal	0.444	0.070
σ	scale factor	0.407	0.021
ν	degrees of freedom	2.28	0.24

Table 4

Comparison of selected models of 19th-century interest rates

Model	# of parameters	Log likelihood	Schwarz criterion
Gaussian AR(2)	5	-932.67	-948.99
Student t AR(2)	6	-677.05	-696.63
Student t AR(2) with MS variance	9	-633.58	-662.95

Note: All models also include cosine seasonal. Schwarz criterion calculated as $L - (k/2) \log(T)$ for L the log likelihood, k the number of parameters, and $T = 682$ the sample size.

Table 5

Maximum likelihood estimates of Markov-switching model for 19th century interest rates

symbol	explanation	MLE	std error
c	typical interest rate	5.11	0.19
ϕ_1	first AR coefficient	1.079	0.040
ϕ_2	second AR coefficient	-0.178	0.039
γ	effect of seasonal	0.441	0.064
σ_1	scale factor in regime 1	0.612	0.019
σ_2	scale factor in regime 2	1.093	0.092
p_{11}	probability regime 1 follows itself	0.9867	0.0068
p_{22}	probability regime 2 follows itself	0.941	0.033
ν	degrees of freedom	4.40	0.90

Table 6

Dates of volatile interest rates and U.S. recessions, 1857-1913

Volatile interest rates	Economic recessions
1857:3-1858:6	1857:6-1858:12
1860:9-1861:11	1860:10-1861:6
——	1865:4-1867:12
1868:3-1874:2	1869:6-1870:2
	1873:10-1879:3
——	1882:3-1885:5
——	1887:3-1888:4
——	1890:7-1891:5
1893:3-1893:12	1893:1-1894:6
1896:7-1896:12	1895:12-1897:6
1898:3-1898:6	——
——	1899:6-1900:12
——	1902:9-1904:8
——	1907:5-1908:6
——	1910:1-1912:1
——	1913:1-1914:12

Table 7

Comparison of selected models of changes in postwar interest rates

Model	# of parameters	Log likelihood	Schwarz criterion
Gaussian AR(2)	4	-292.30	-304.88
Student t AR(2)	5	-150.66	-166.38
Student t AR(2) with MS variance	8	-87.96	-113.13

Note: Schwarz criterion calculated as $L - (k/2) \log(T)$ for L the log likelihood, k the number of parameters, and $T = 540$ the sample size.

Table 8

Maximum likelihood estimates of Markov-switching model for changes in postwar interest rates

symbol	explanation	MLE	std error
c	intercept	0.0016	0.0096
ϕ_1	first AR coefficient	0.409	0.049
ϕ_2	second AR coefficient	-0.046	0.042
σ_1	scale factor in regime 1	0.174	0.013
σ_2	scale factor in regime 2	0.740	0.107
p_{11}	probability regime 1 follows itself	0.9941	0.0049
p_{22}	probability regime 2 follows itself	0.9635	0.0247
ν	degrees of freedom	4.27	0.94

Figure Captions

Figure 1. U.S. monthly civilian unemployment rate and U.S. recessions, 1948:1-2004:3.

Figure 2. Estimated spectrum of U.S. monthly civilian unemployment rate, 1948:1-2004:3, plotted as a function of period of the cycle in years.

Figure 3. A simulated sample generated from equation (4).

Figure 4. Smoothed probabilities for moderate recession regime ($\Pr(s_t = 2|y_1, y_2, \dots, y_T; \hat{\theta})$ in second panel) and severe recession regime ($\Pr(s_t = 3|y_1, y_2, \dots, y_T; \hat{\theta})$ in third panel) for $\hat{\theta}$ the maximum likelihood estimates reported in Table 2. First panel reproduces the unemployment data from Figure 1.

Figure 5. Simulated time path for unemployment under three scenarios. First panel: unemployment is initially at 6% and the economy remains in regime 1 with no further shocks. Second panel: unemployment is initially at 3% and the economy remains in regime 2 with no further shocks. Third panel: unemployment is initially at 6% and the economy remains in regime 3 with no further shocks. Horizontal axis in each panel measures months from the initial condition.

Figure 6. Monthly short-term commercial paper rates in New York City, 1857:1-1937:1.

Figure 7. Estimated spectrum of U.S. monthly short-term commercial paper rate, 1857:1-1913:12, plotted as a function of the period of the cycle in years.

Figure 8. First panel reproduces the interest rate data from Figure 6 for 1857:1-1913:12. Second panel: smoothed probability for high-volatility interest rate regime, $\Pr(s_t = 2|y_1, y_2, \dots, y_T; \hat{\theta})$ for $\hat{\theta}$ the maximum likelihood estimates reported in Table 5. Third panel: same series as

in second panel with NBER recessions indicated as shaded areas.

Figure 9. Top panel: U.S. 6-month Treasury bill rates and U.S. recessions, 1958:12-2004:4. Bottom panel: smoothed probability for high-volatility interest rate regime, $\Pr(s_t = 2 | y_1, y_2, \dots, y_T; \hat{\theta})$ for $\hat{\theta}$ the maximum likelihood estimates reported in Table 8

Figure 1. Unemployment

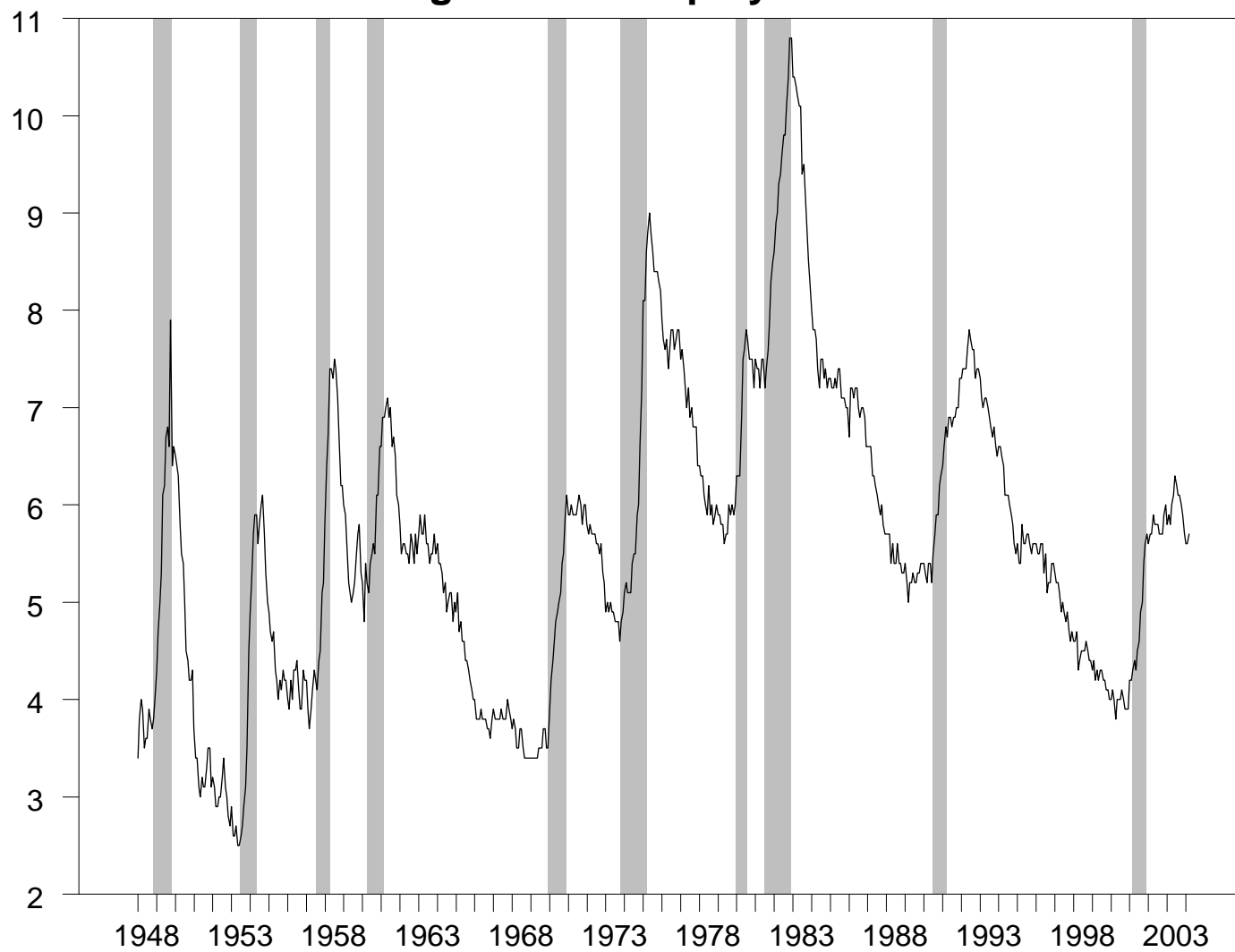


Figure 2.
Spectrum of the Unemployment Rate

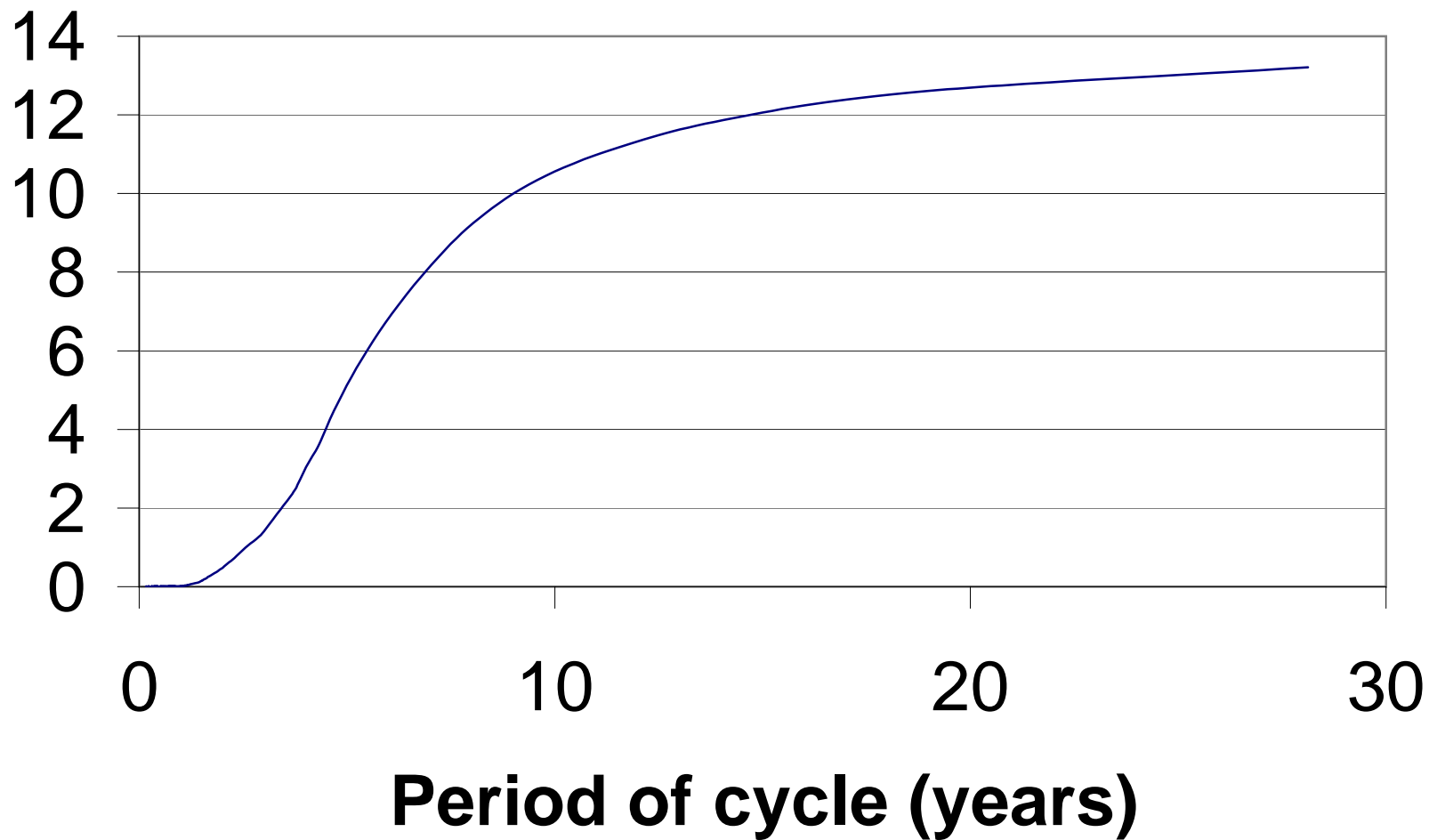


Figure 3. Simulated Unemployment

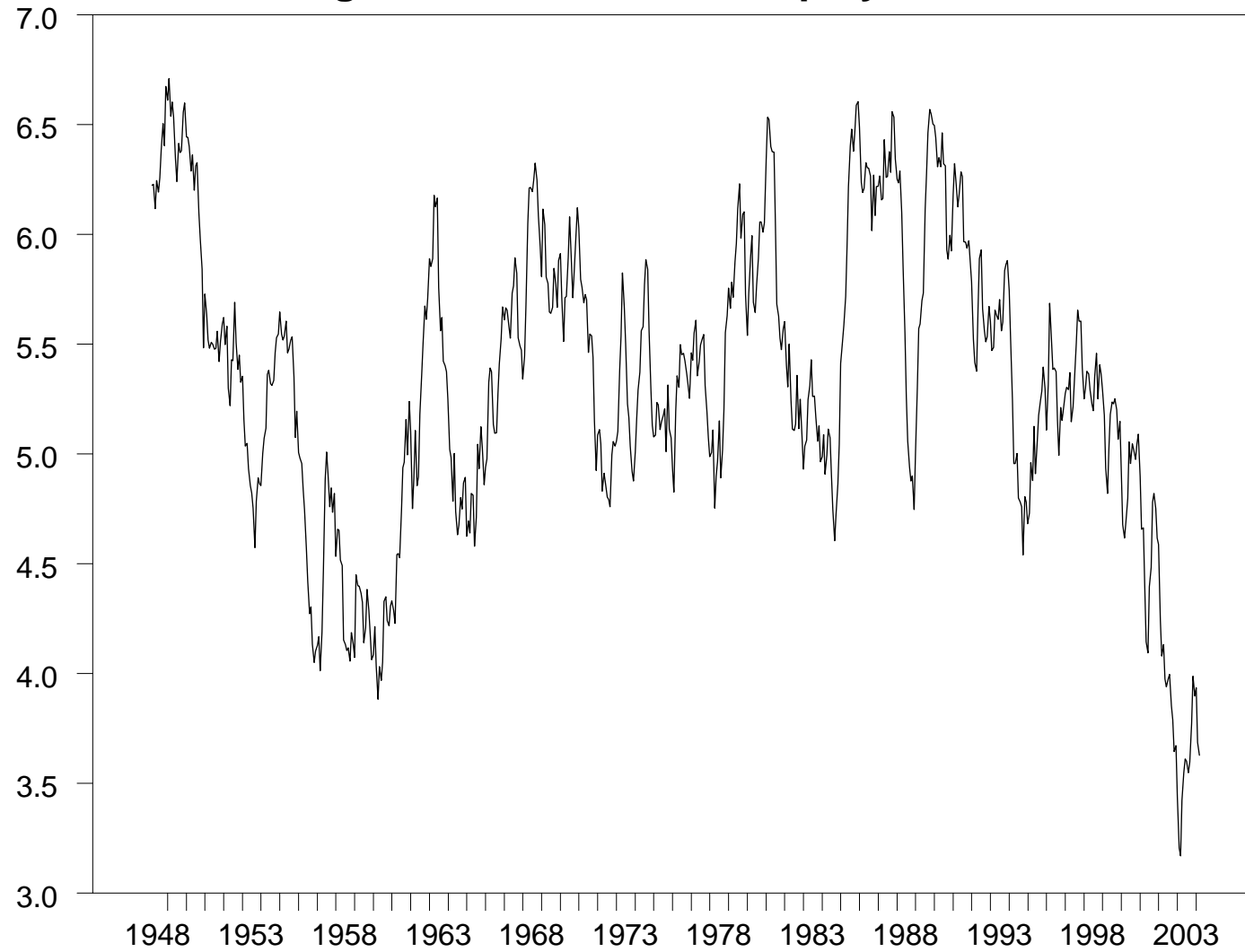
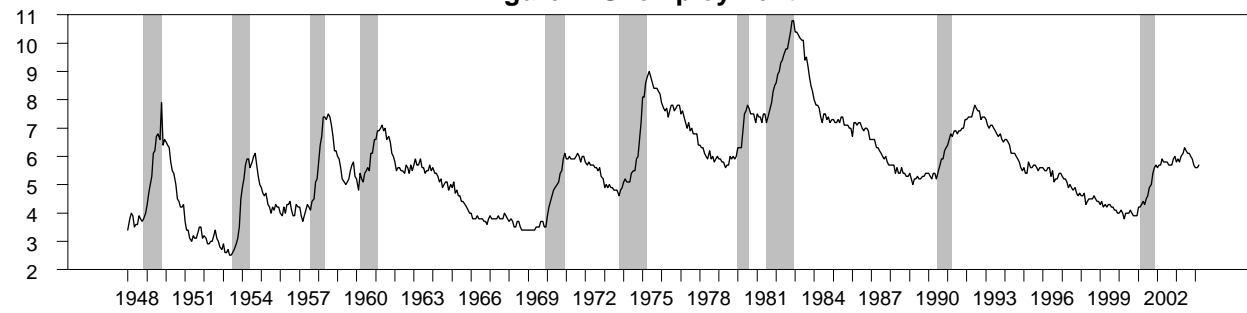
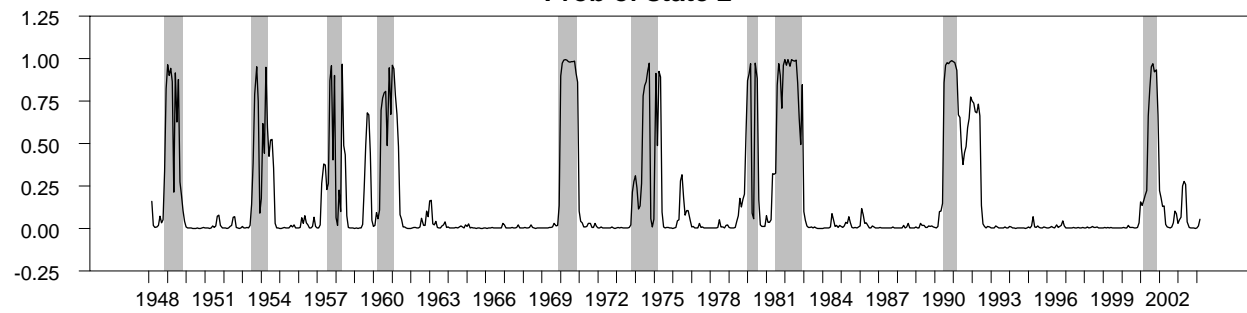


Figure 4. Unemployment



Prob of state 2



Prob of state 3

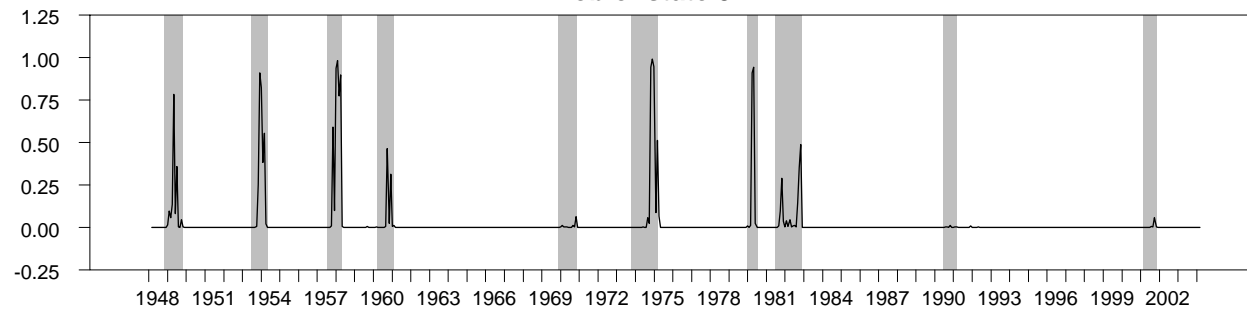
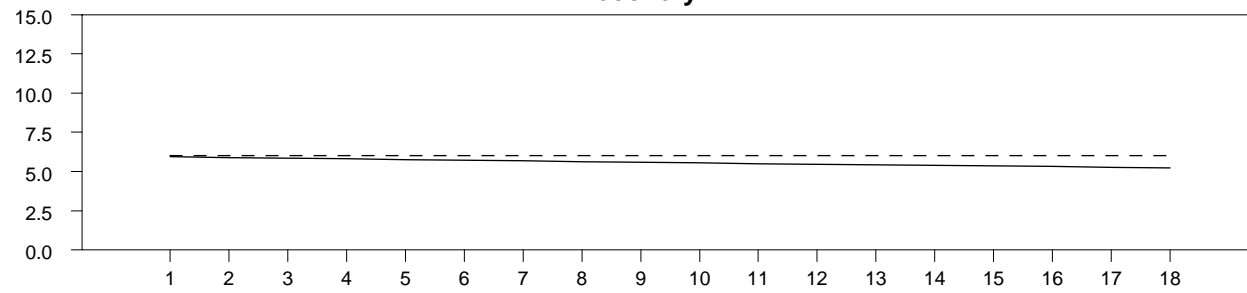
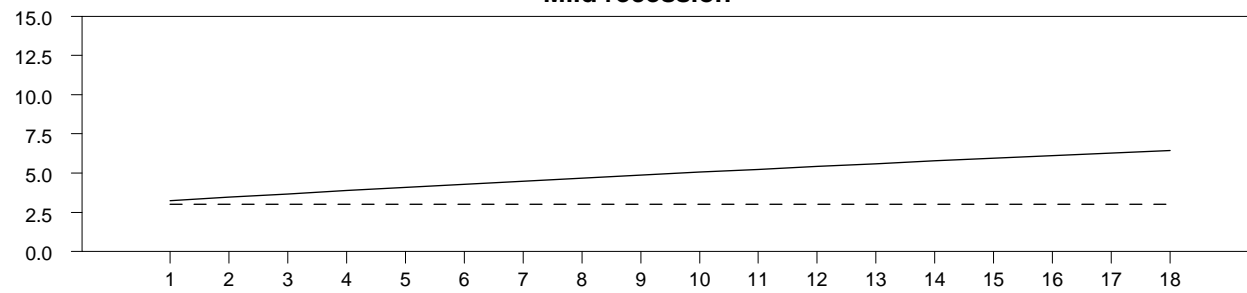


Figure 5

Recovery



Mild recession



Severe recession

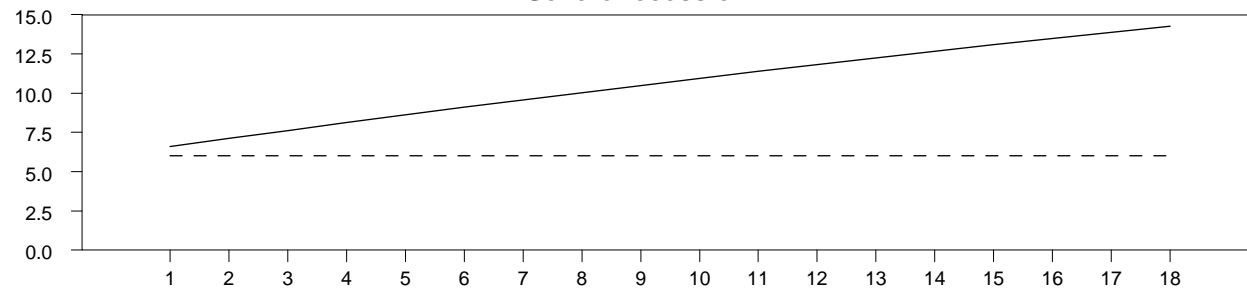


Figure 6. Commercial paper rates in New York City

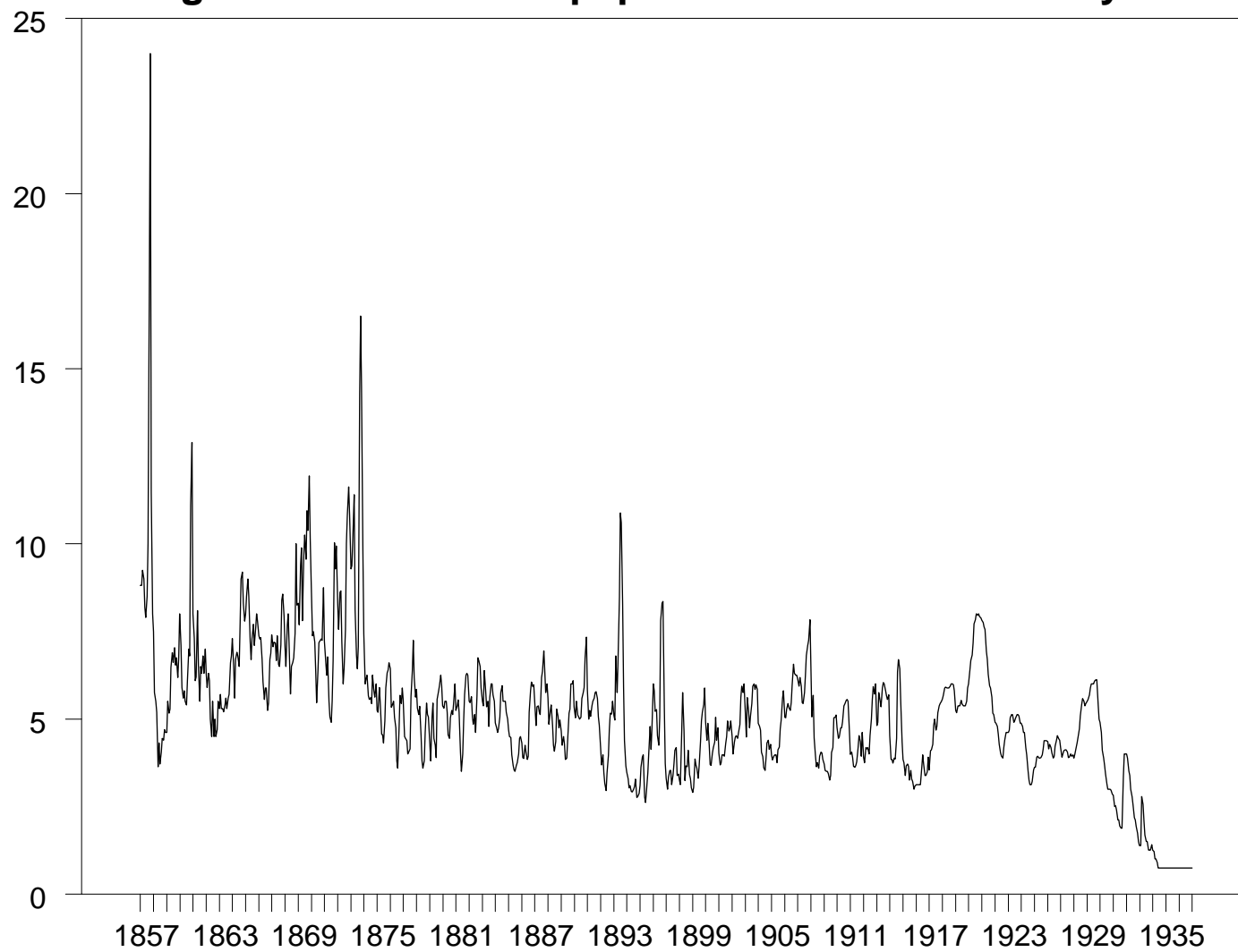


Figure 7
Spectrum of 19th Century Interest Rates

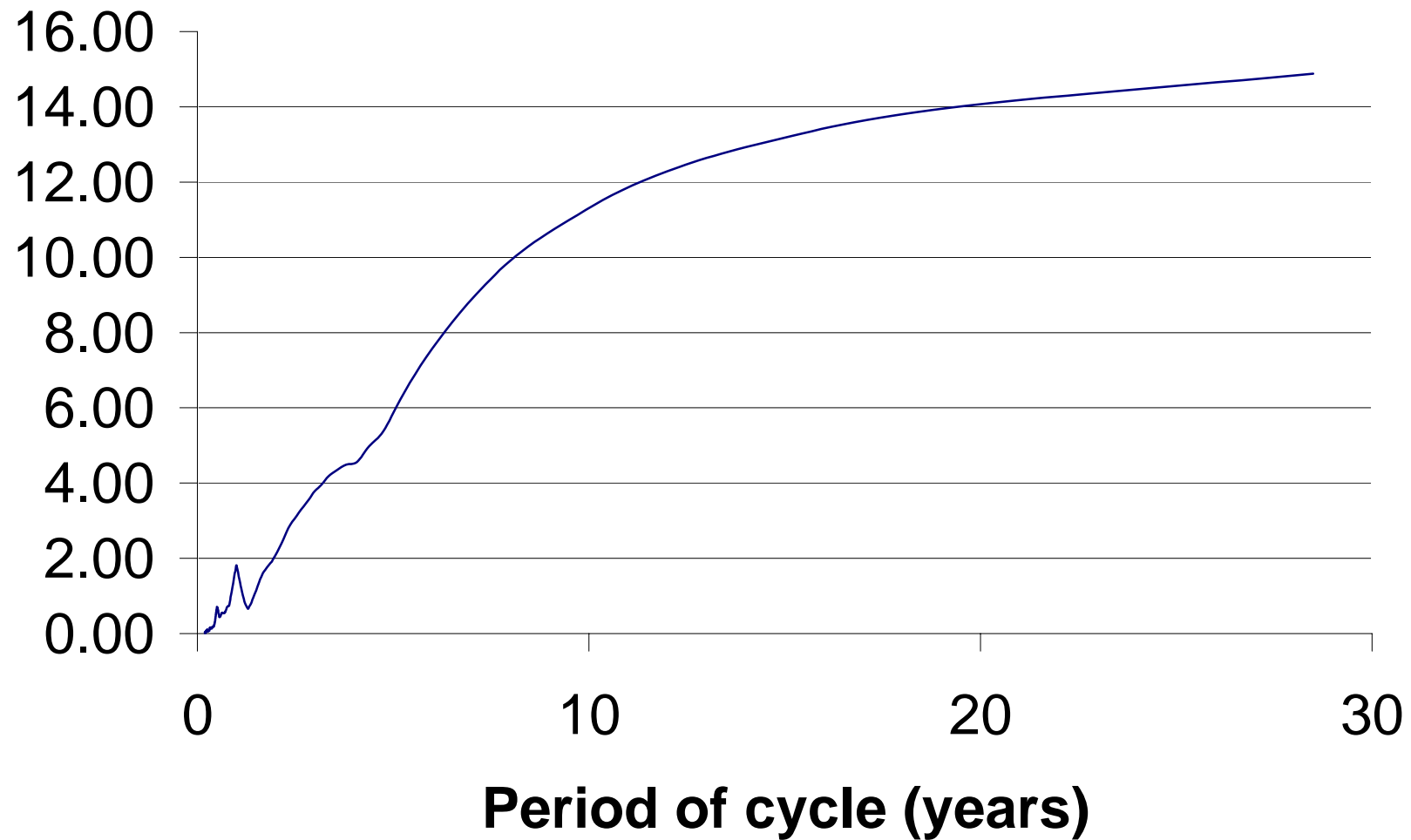
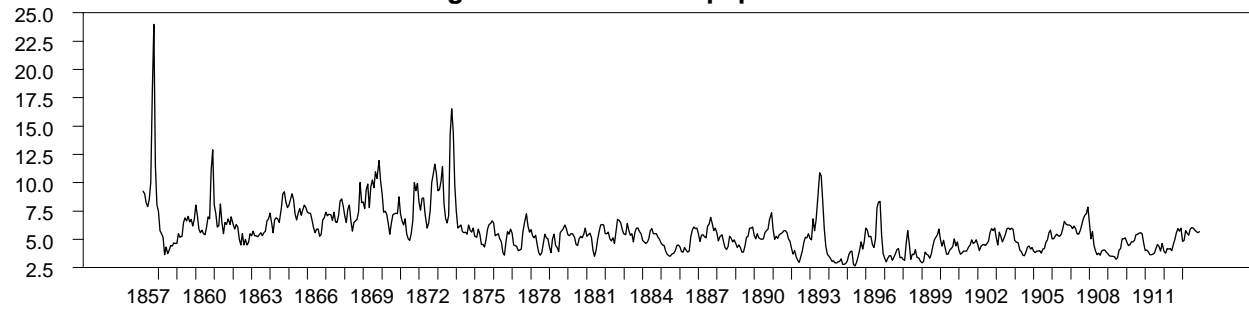
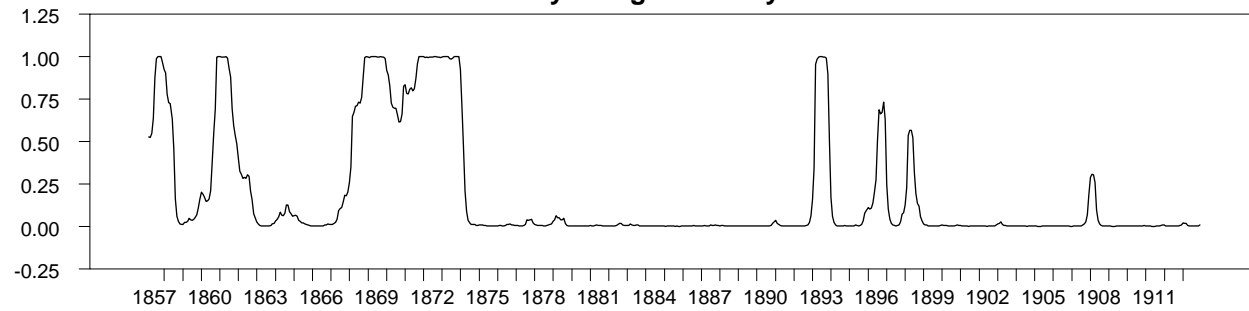


Figure 8. Commercial paper rates



Probability of high volatility state



NBER recessions

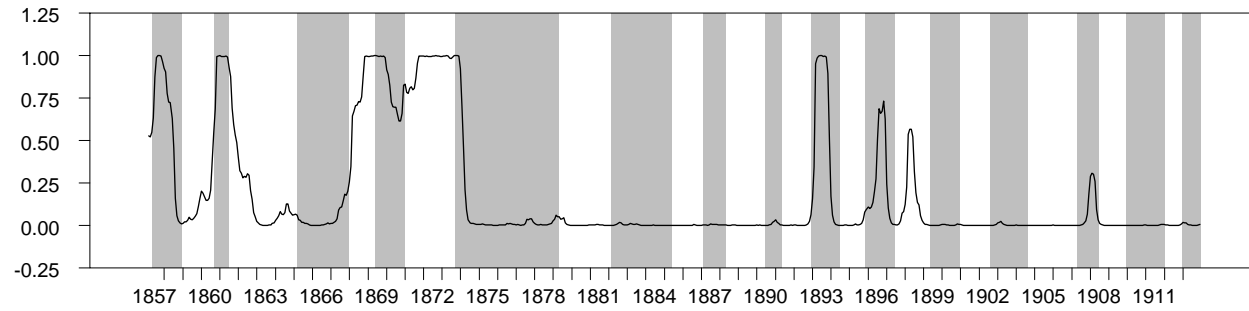
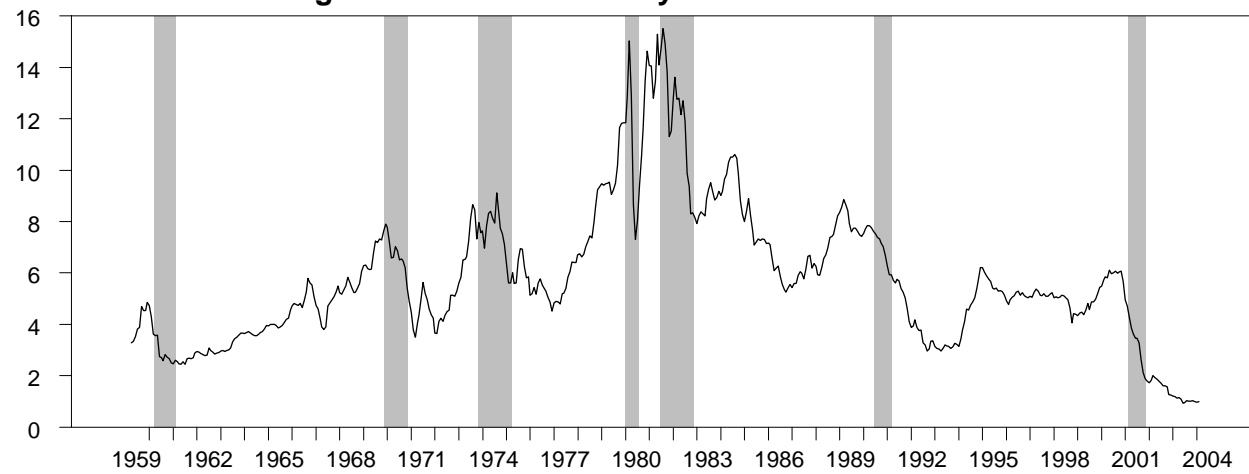


Figure 9. 6-month treasury rates and recessions



Probability of high volatility state and recessions

